

TL 9-46 (Vibrational spectrum of hydrogen molecule)

a) For an  $H_2$  molecule,

$$\mu = \frac{m_1 m_2}{m_1 + m_2} = 0.5 \text{ amu}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} = \frac{1}{2\pi} \sqrt{\frac{580 \text{ N/m}}{0.5 \text{ amu}}} = 133 \text{ THz}$$

$$\lambda_{\text{photon}} = 2.25 \text{ } \mu\text{m}$$

for transition between  
any 2 energy levels

b) for  $H-D$  molecule

$$\mu = 0.67 \text{ amu}$$

$$f = 115 \text{ THz}$$

$$\lambda = 2.61 \text{ } \mu\text{m}$$

c) for  $D-D$  molecule

$$\mu = 1.6667 \text{ amu}$$

$$f = 94 \text{ THz}$$

$$\lambda = 3.19 \text{ } \mu\text{m}$$