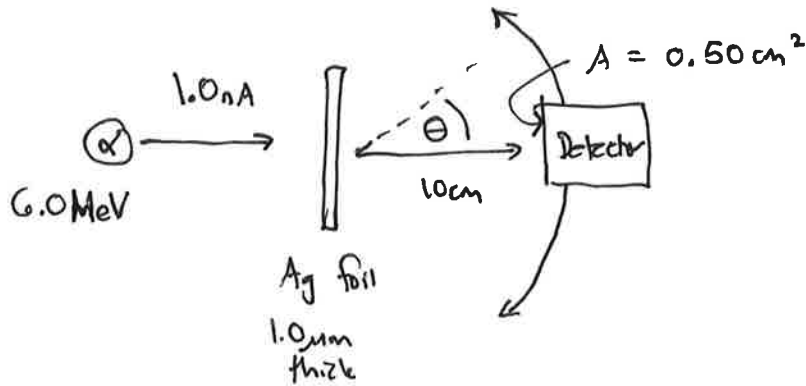


TL 4-48



How many α -particles will be scattered per second into the detector at (a) $\theta = 60^\circ$? (b) $\theta = 120^\circ$

Use $\Delta N = \left(\frac{I_0 A_{sc} n t}{r^2} \right) \left(\frac{k Z e^2}{2 E_\alpha} \right)^2 \frac{1}{\sin^4\left(\frac{\theta}{2}\right)}$

Annotations:
 I_0 : current
 A_{sc} : detector area
 n : # nuclei per unit volume
 t : thickness of foil
 r^2 : distance to detector
 $\frac{k Z e^2}{2 E_\alpha}$: \propto ptcl KE
 $\frac{1}{\sin^4(\frac{\theta}{2})}$: unit area of incident beam

- There are a few as-yet-undetermined values in this formula.
- So: for silver: $Z = 47$

$$n = \frac{\rho N_A}{M} = \frac{(10.49 \text{ g/cc}) (6.02 \times 10^{23} \text{ atoms/mol})}{(107.9 \text{ g/mol})} = 5.85 \times 10^{28} \frac{\text{atoms}}{\text{m}^3}$$

$$I_0 = \frac{\text{current}}{\text{charge/ptcl area}} = \frac{1.0 \times 10^{-9} \text{ coul/sec}}{2(1.6 \times 10^{-19} \text{ coul}) \text{ area}} = \frac{3.1 \times 10^9}{\text{sec} \cdot \text{area}}$$

• Plugging in numbers gives

$\Delta N_{60^\circ} = 465 \text{ } \alpha\text{-ptcls/second at } 60^\circ$
$\Delta N_{120^\circ} = 52 \text{ } \alpha\text{-ptcls/second at } 120^\circ$